

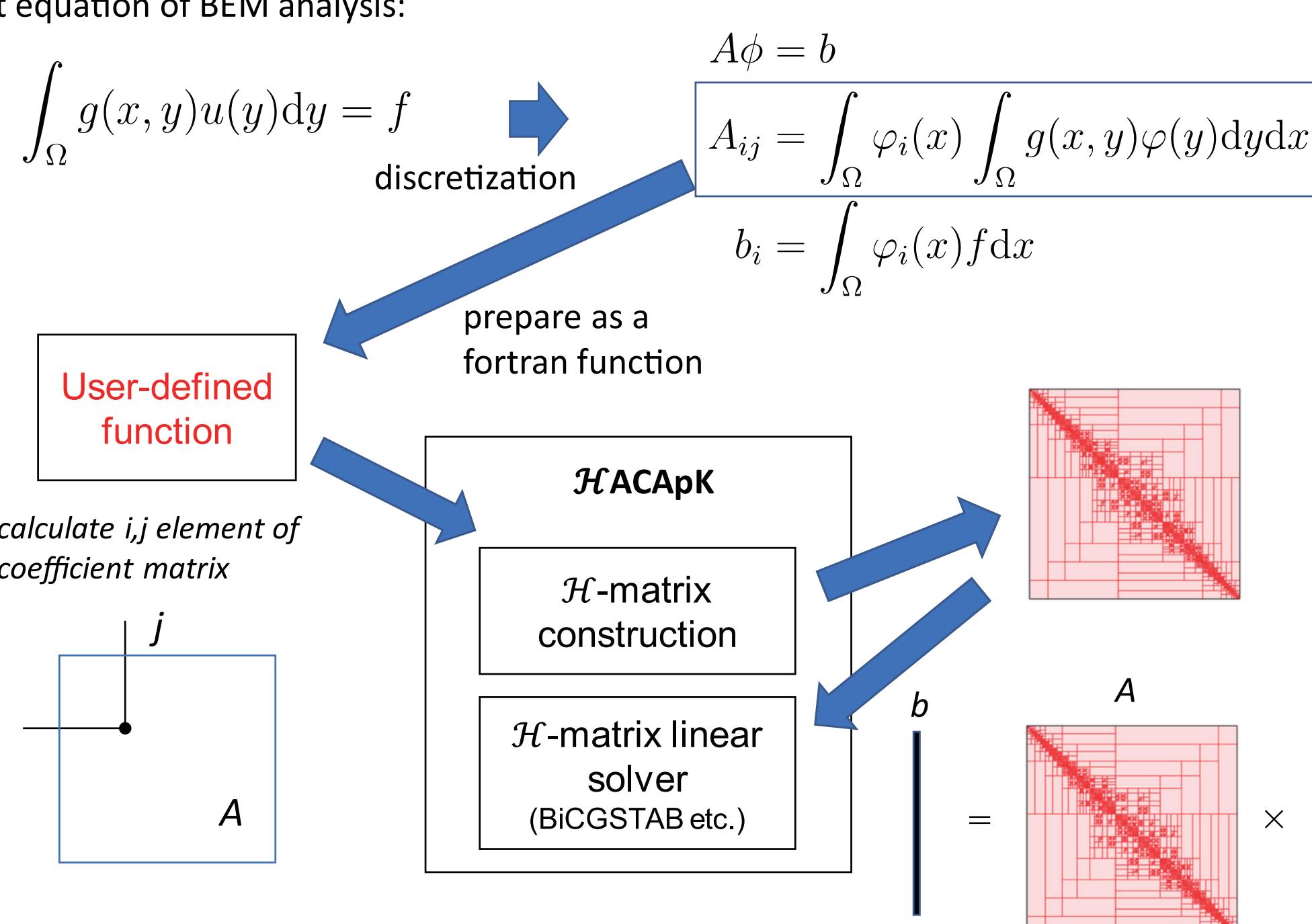
HACApK for Many-core Processors

Tetsuya Hoshino

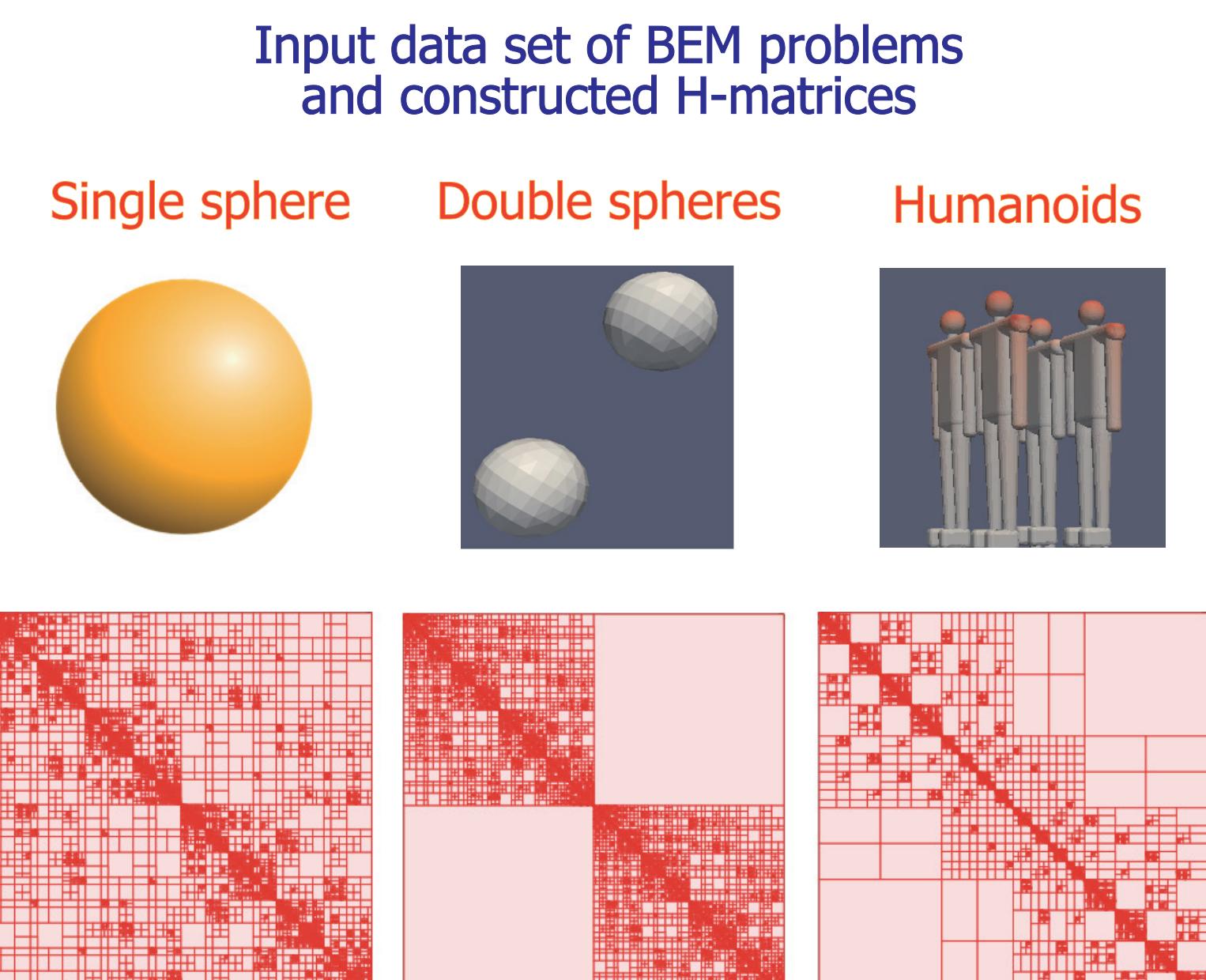
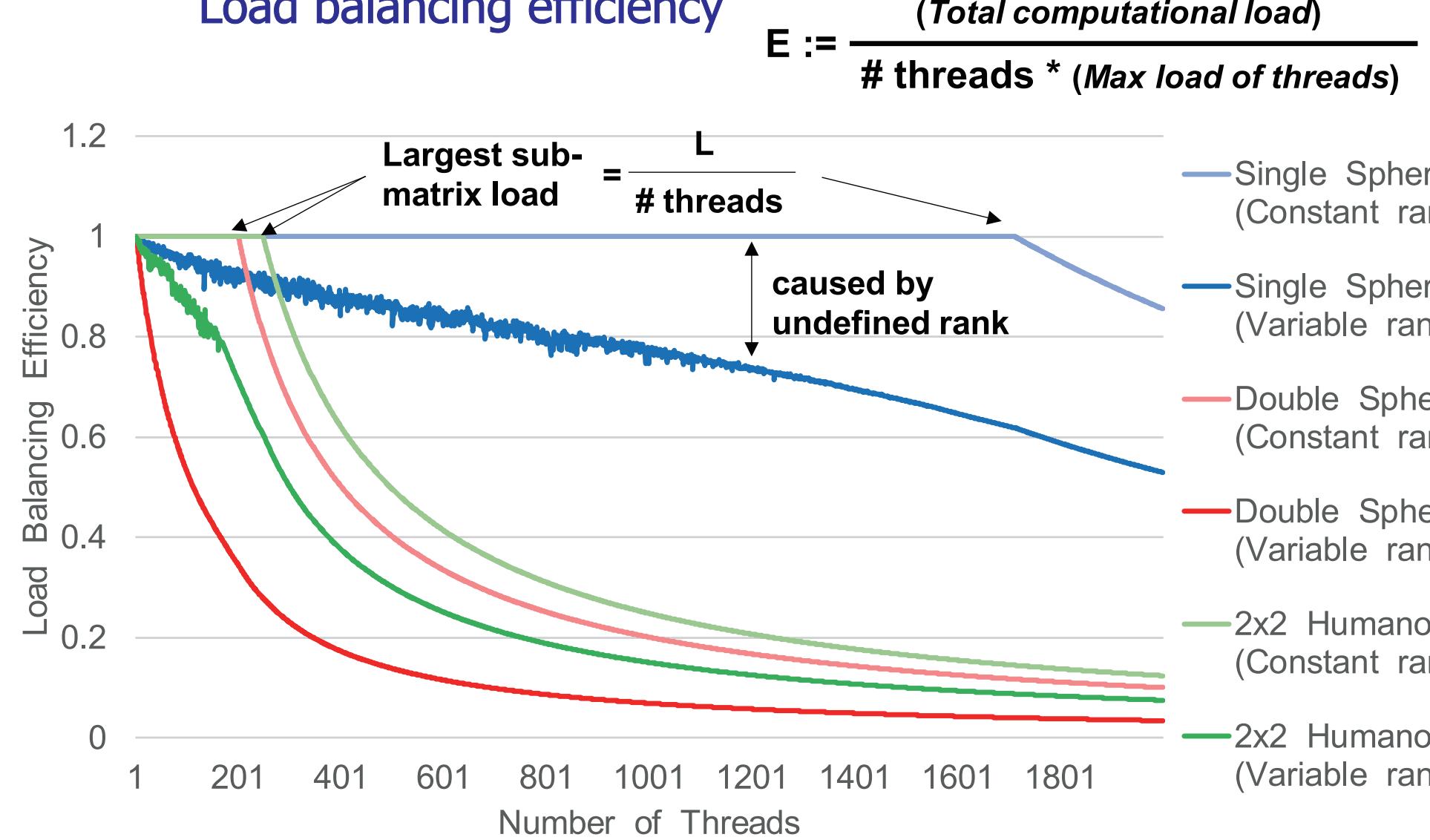
Overview of HACApK

- Fortran90 based library for H-matrices
- H-matrices: Approximation technique for dense matrices
- Provides parallel generation of H-matrix and parallel linear solvers

Target equation of BEM analysis:



Load balancing efficiency

$$E := \frac{\text{(Total computational load)}}{\# \text{ threads} * (\text{Max load of threads})}$$


Load-balancing-aware Algorithms for GPUs

Tetsuya Hoshino, Akihiro Ida, Toshihiro Hanawa and Kengo Nakajima, "Load-balancing-aware Parallel Algorithms of H-matrices with Adaptive Cross Approximation for GPUs", IEEE Cluster 2018, Belfast, UK (September 10-13, 2018)

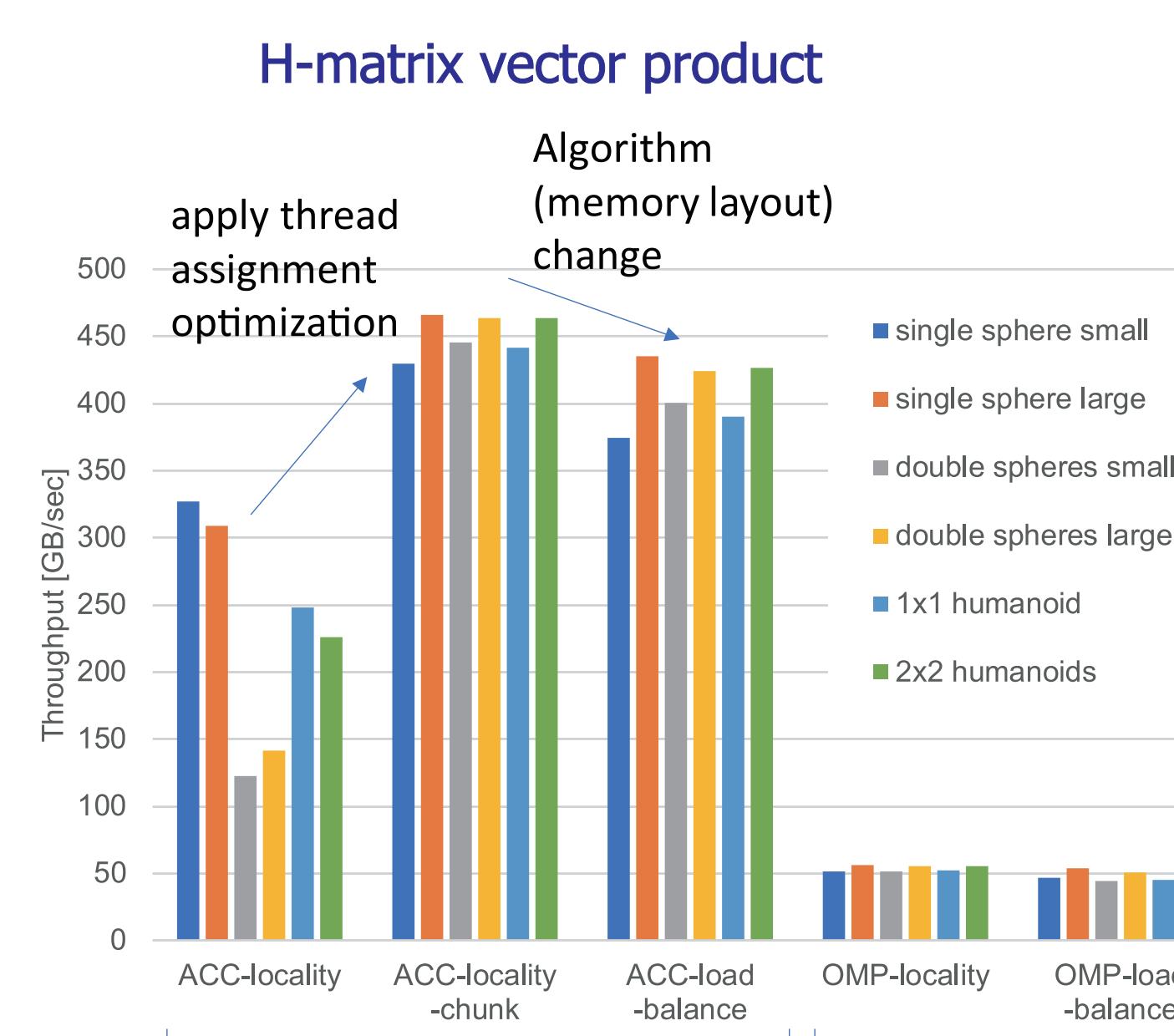
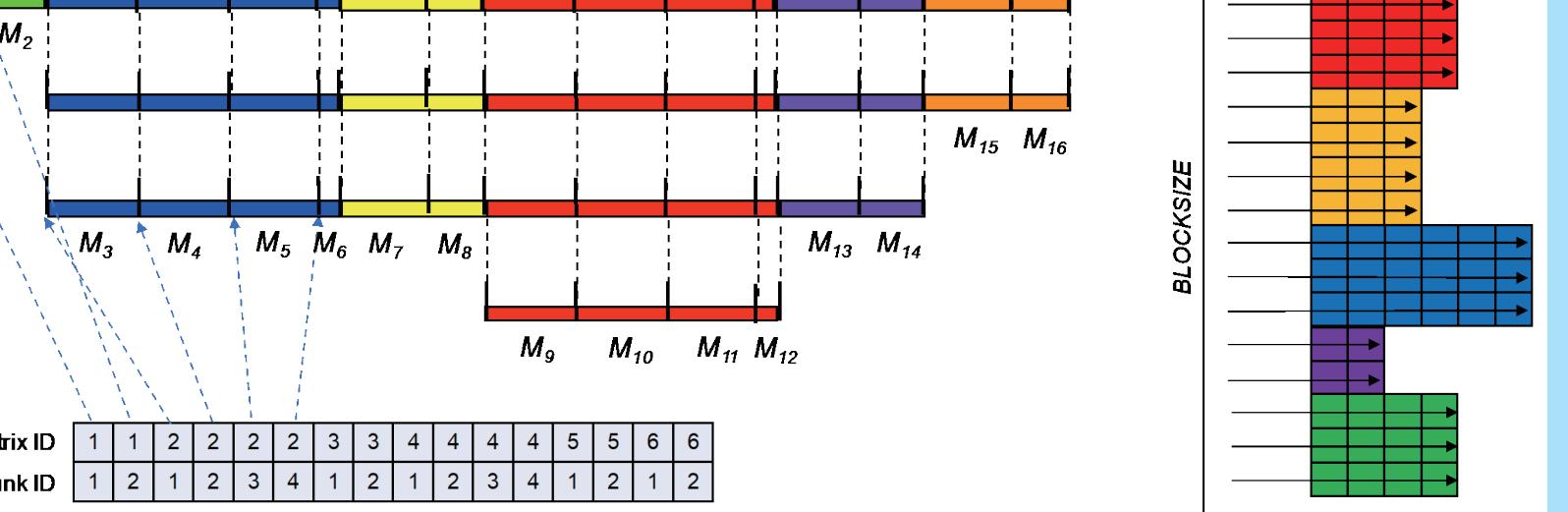
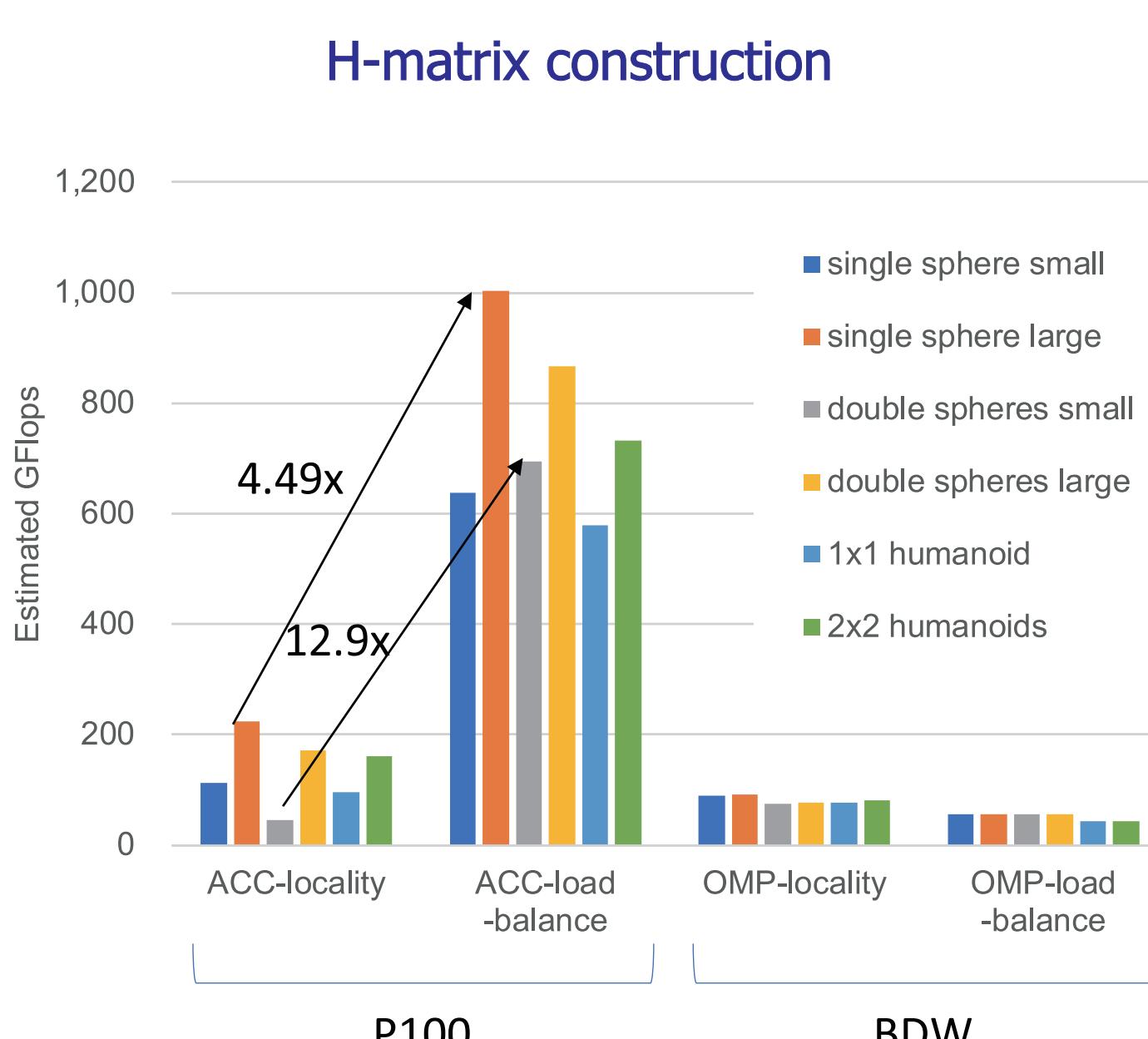
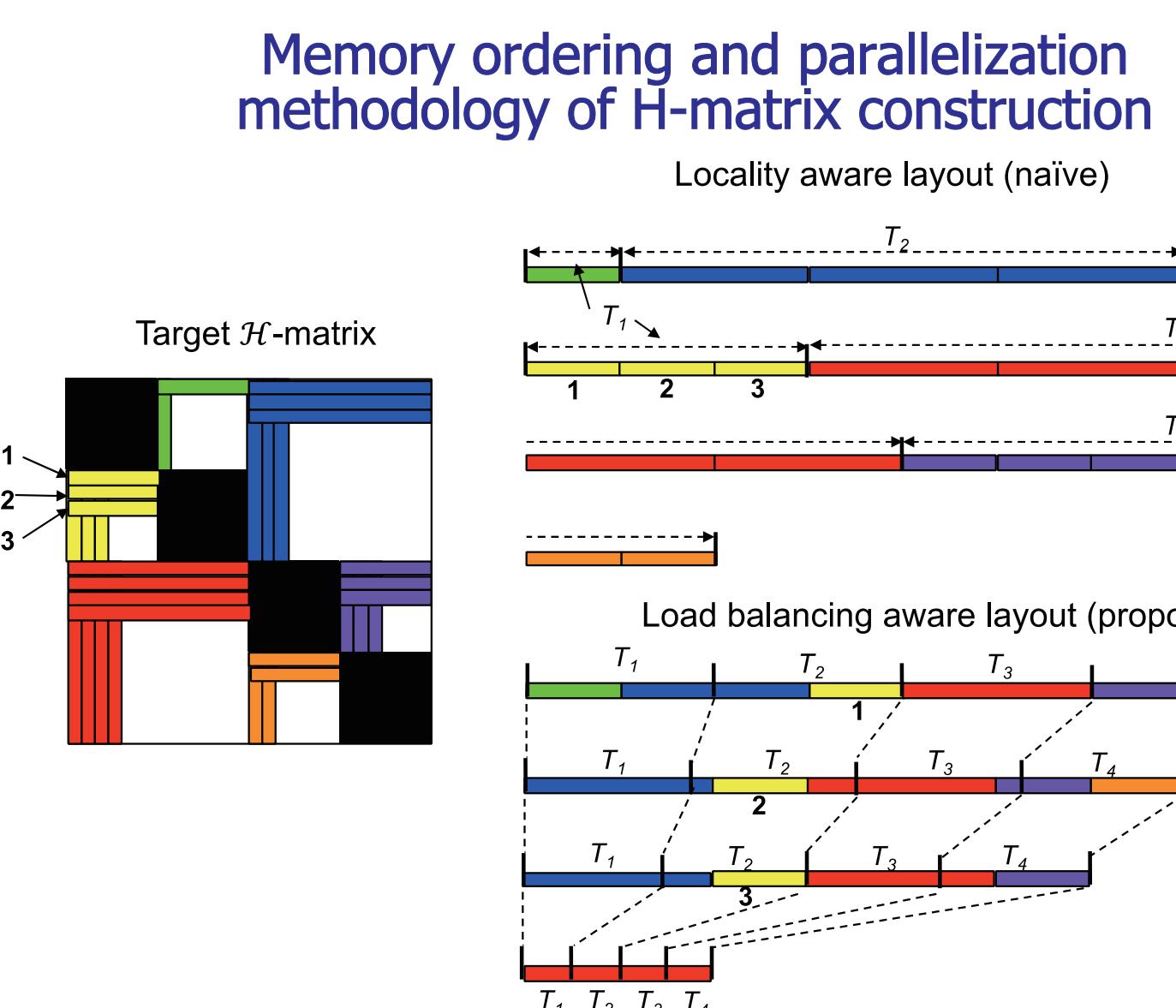
- We propose load-balancing-aware H-matrix construction with ACA
- ACA process is concurrently applied to all sub-matrices
- We implemented the proposed algorithm into HACApK
- Evaluated on NVIDIA Tesla P100 and Intel Xeon Broadwell (BDW) with electrostatic field analyses

H-matrix construction with ACA

```

FOR ALL sub-matrices DO
    choose first column vector
    DO k = 1, KMAX
        FOA ALL column vector element DO
            calculate i, j element with userfunc
            subtract the summation of 1,2,...,k-1 element
        ENDO
        calculate max of kth column
        FOA ALL row vector element DO
            calculate i, j element with userfunc
            subtract the summation of 1,2,...,k-1 element
        ENDO
        calculate error
        IF(error < eps) EXIT
        calculate max of kth row
    ENDDO
    ENDDO

```



Semi-auto-vectorization for Wide SIMD Processors

Tetsuya Hoshino, Akihiro Ida, Toshihiro Hanawa and Kengo Nakajima, "Design of Parallel BEM Analyses Framework for SIMD Processors", The International Conference on Computational Science 2018 (ICCS 2018), Wuxi, China

- We propose new design of user function interface of HACApK
 - Enhance compiler vectorization without SIMD knowledge
- We implemented the proposed design into HACApK
 - Evaluated on Intel Xeon Phi KNL and Intel Xeon Broadwell (BDW) with electrostatic field analyses

Parallelization of H-matrix construction with OpenMP directives

```

subroutine hmat_generation(st_bemv)
type(hacapkInput)::st_bemv
!$omp parallel do
do submat = 1, numSubmat
    ...
    !$omp simd
    do i = str, enr
        a(i,j) = user_func(i,j,st_bemv)
    end do
    ...
end do
end subroutine hmat_generation

```

User function caller

User function callee

Data access

```

subroutine set_args(i,j,st_bemv,a1,a2,...)
integer :: i,j
type(hacapkInput)::st_bemv
real(8)::a1,a2, ...
a1 = st_bemv%a1(i,j)
a2 = st_bemv%a2(i,j)
...
end subroutine set_args

```

Original interface

Computation

```

real(8) function user_func(i,j,st_bemv)
integer :: i,j
type(BemInput)::st_bemv
real(8)::a1,a2, ...
a1 = st_bemv%a1(i,j)
a2 = st_bemv%a2(i,j)
...
! calculate i,j value of coefficient
end function user_func

```

User implementation

```

real(8) function vectorize_func(a1,a2,...)
!$omp declare simd(vectorize_func)
!$omp SIMDLENGTH
ans(ii) = vectorize_func(arg1(ii),arg2(ii),...)
end do
do ii = 1,SIMDLENGTH
    ans(ii) = vectorize_func(arg1(ii),arg2(ii),...)
end do
do ii = 1,SIMDLENGTH
    a(i,j) = ans(ii)
end do
end do

```

Automatically inserted by framework

Electrostatic field analysis with single sphere conductor

- We use two user-defined functions
 - Perfect conductor $P[u]$ without branch
 - Dielectric $D[u]$ with branch divergent

$$\mathcal{P}[u](x) := \int_{\Omega} \frac{1}{4\pi \|x - y\|} u(y) dy, x \in \Omega$$

$$\mathcal{D}[u](x) := \int_{\Omega} \frac{\langle x - y, n(y) \rangle}{4\pi \|x - y\|^3} u(y) dy, x \in \Omega$$

