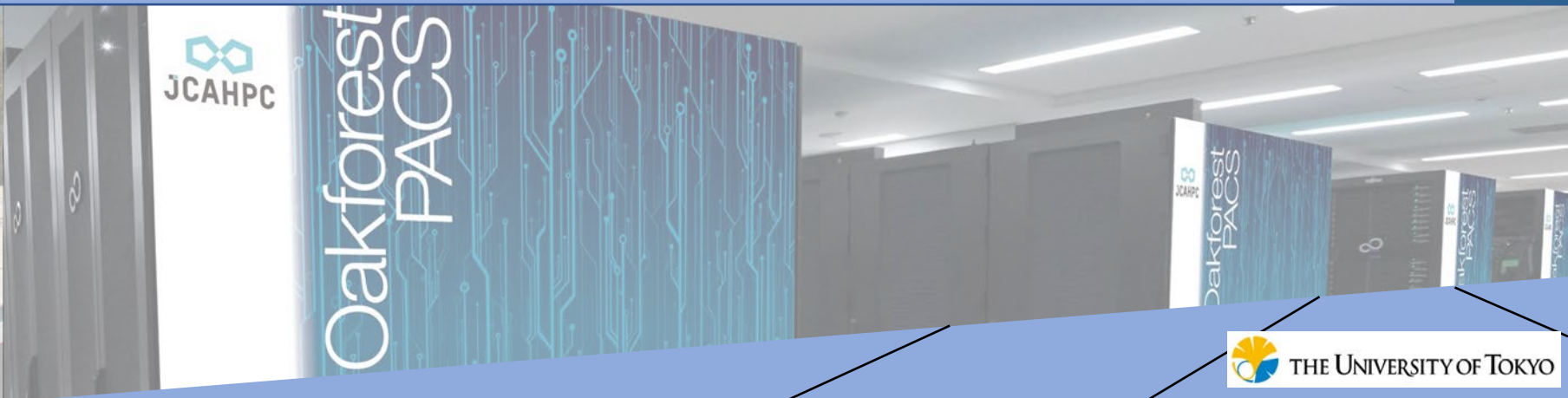




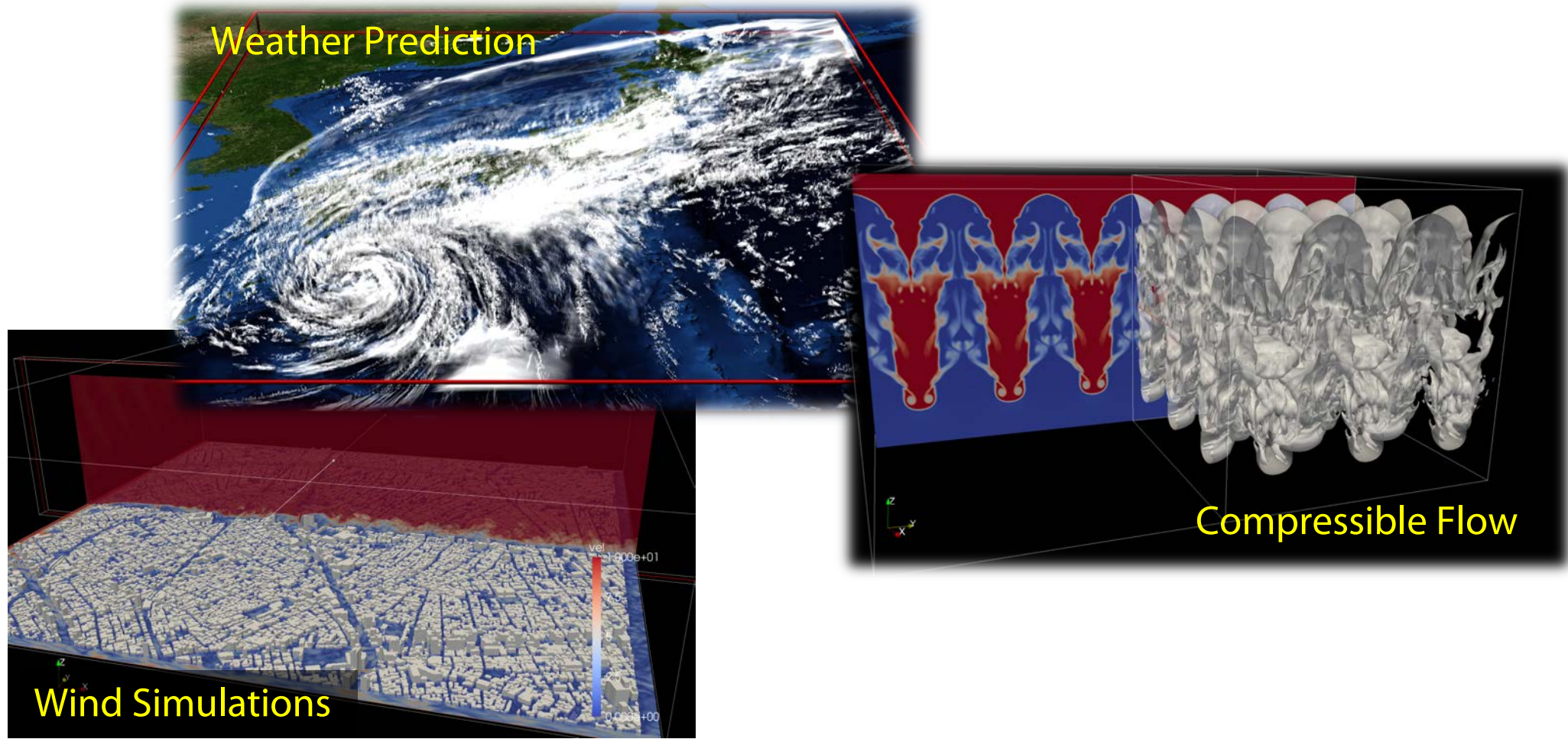
# Fast Surrogate for Approximating Steady Flow Simulations

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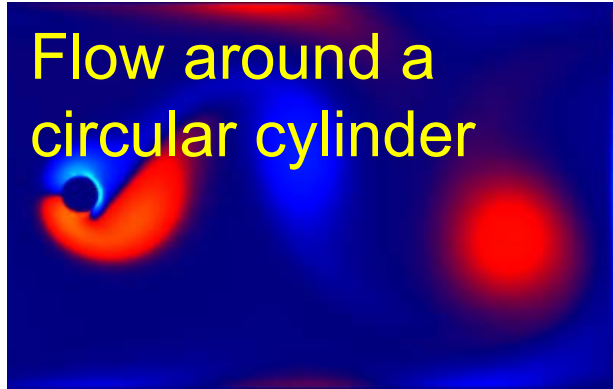
# Computational Fluid Dynamics



- Computational cost of computational fluid dynamics is relatively high.  
➡ **Fast surrogate based on deep neural networks (DNNs)  
for approximating steady flow simulations**

## Dataset

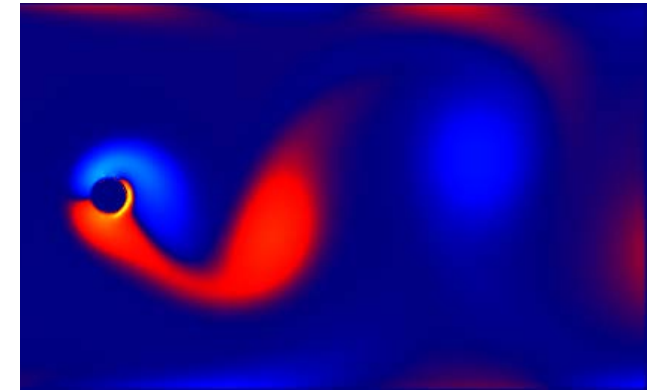
Flow around a circular cylinder



CFD simulation  
(Lattice Boltzmann  
methods)

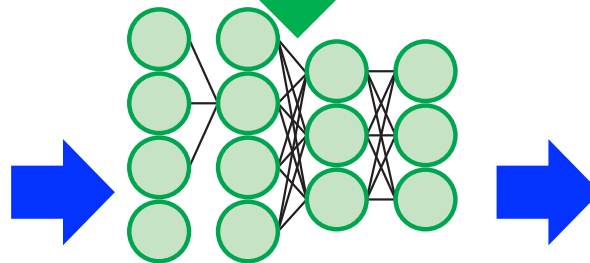
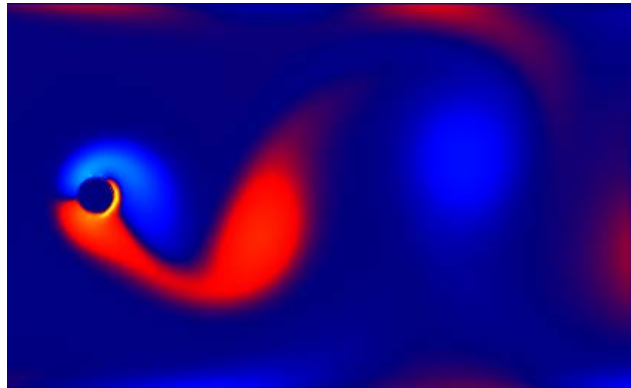


$$f_i(x + c_i \Delta t, t + \Delta t) = f_i(x, t) + \Omega_i(x, t)$$
$$\Omega_i(x, t) = -\frac{1}{\tau} (f_i(x, t) - f_i^{eq}(x, t))$$



## Training

## Prediction



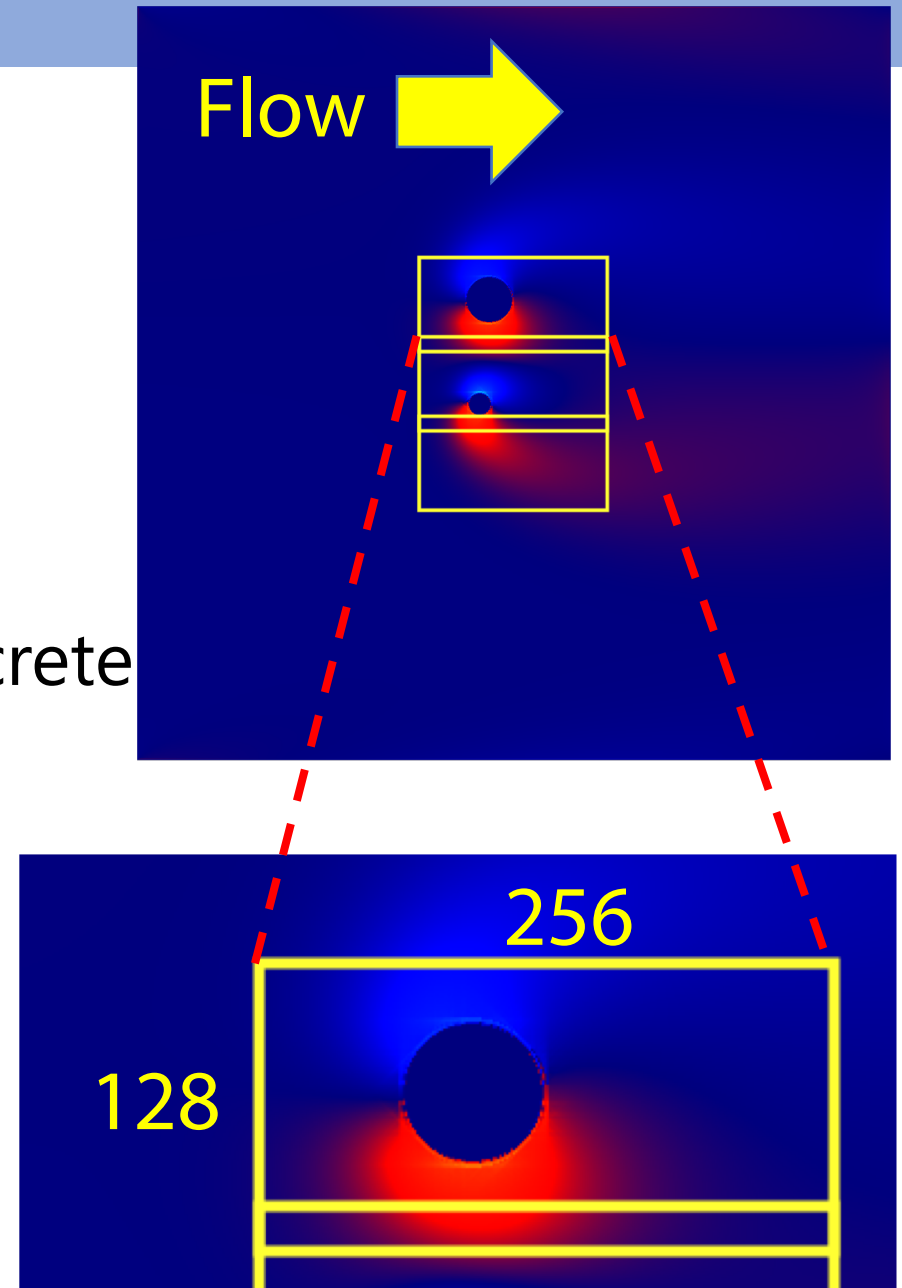
Convolutional neural networks (CNNs)  
to predict simulation results

Prediction of flow

**CNNs may become “faster simulator”**

# Datasets

- Steady flow
  - The fluid flows along the x axis around objects.
- LBM simulation results
  - D2Q9 model (9 variables is used for discrete velocity)
  - $Re = 100$ , Domain size:  $1024 \times 1024$
  - Random sized cylinders
- Input data:  $256 \times 128$  (clipped)
  - Training: 4608
  - Validation: 1536



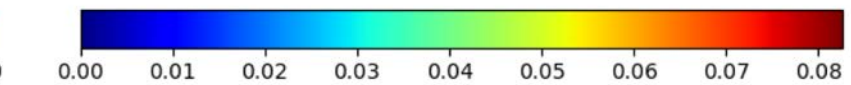
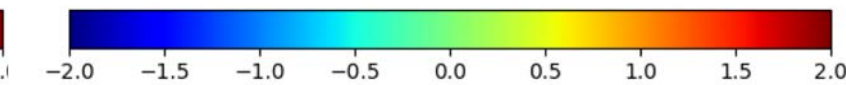
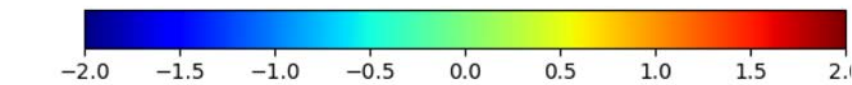
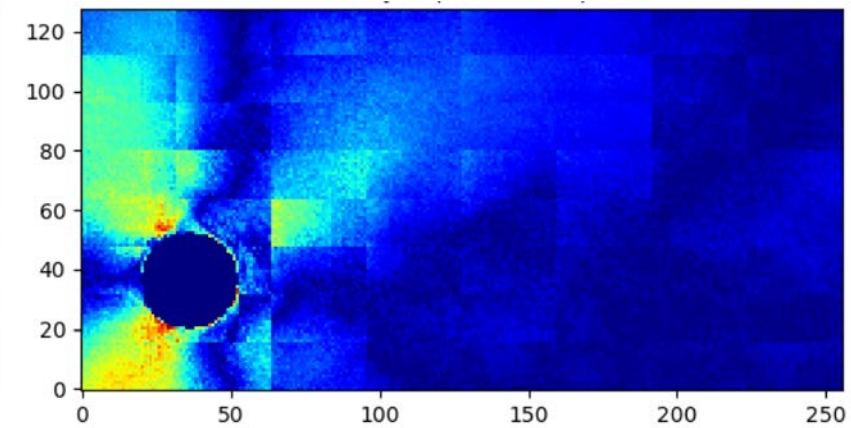
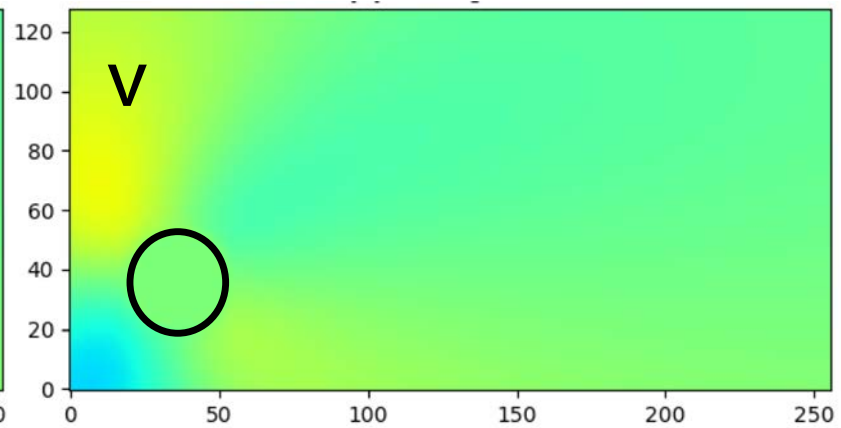
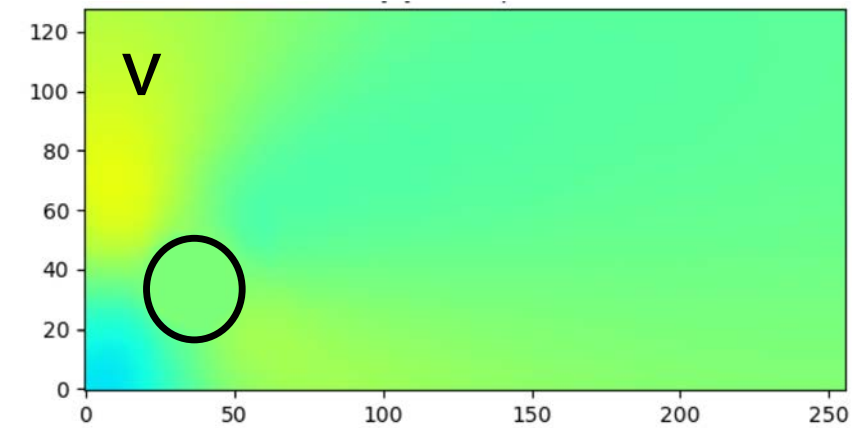
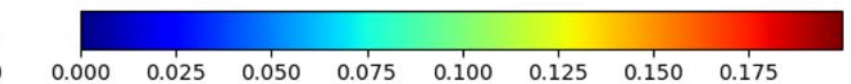
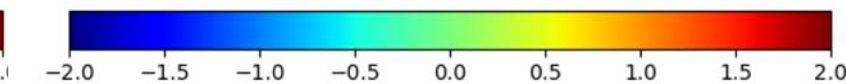
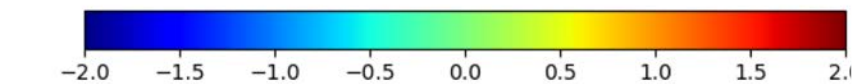
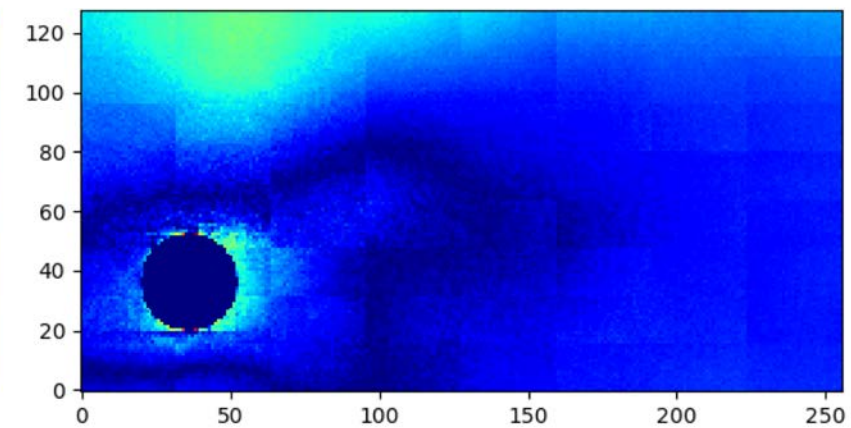
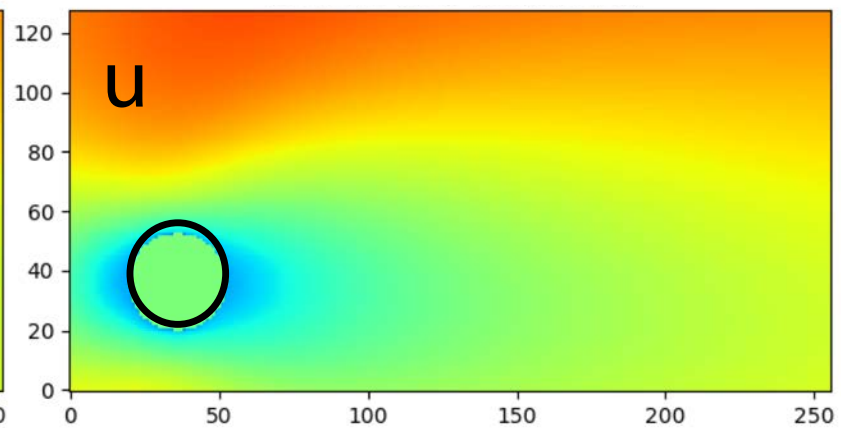
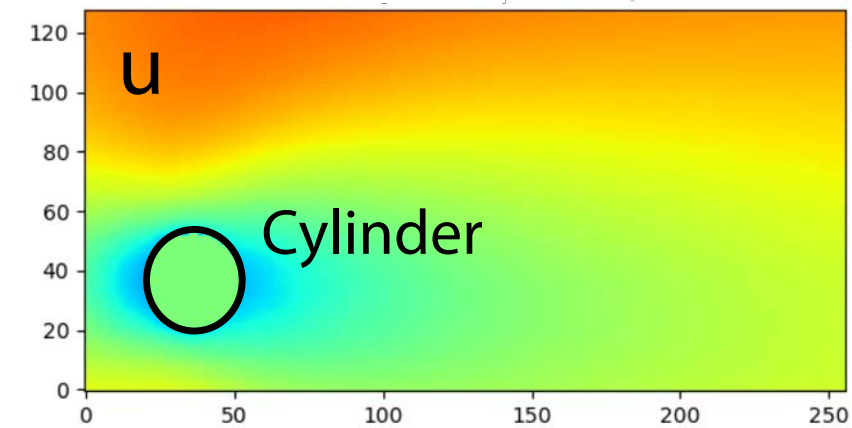


# Prediction results for single domain

**CNN Prediction**

**LBM Ground truth**

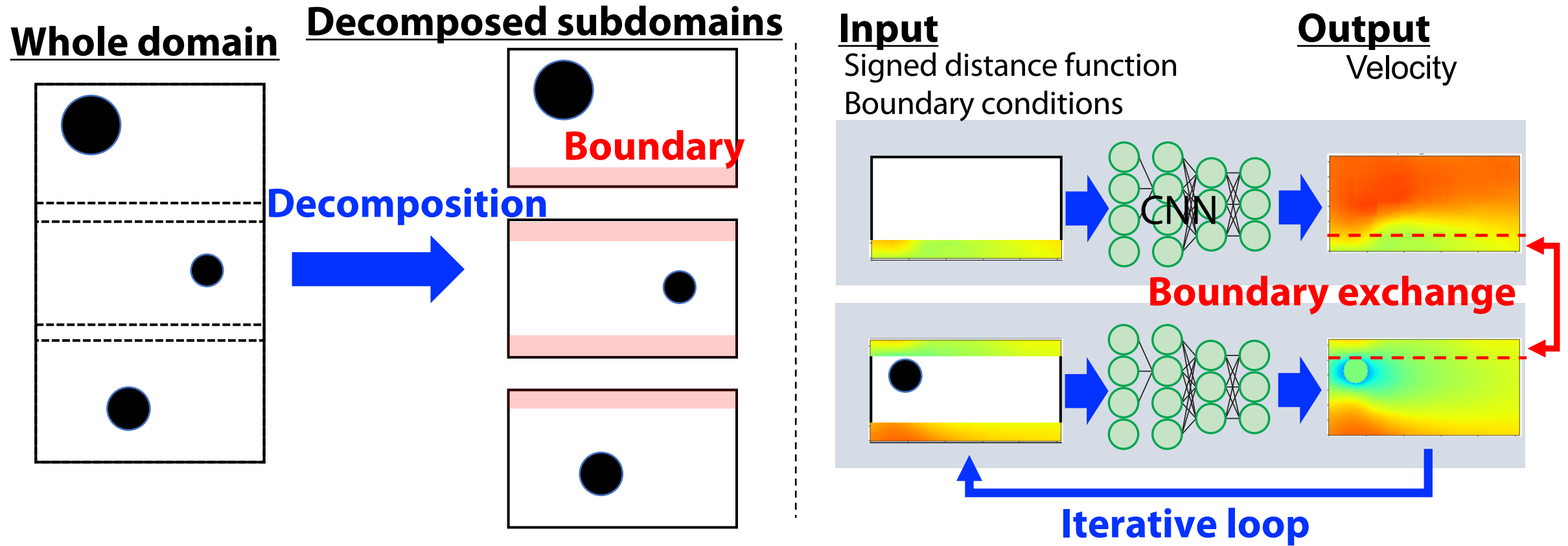
**Err = |CNN - LBM|**



Loss:  $7.3 \times 10^{-5}$

# Prediction by CNN with boundary exchange

- The network model trained for a single domain is applied to the decomposed subdomains to predict the simulation results in each subdomain.
- In order to maintain consistency between values in the subdomains, boundary exchange between neighbor subdomains is performed.
- CNN and boundary exchange are performed iteratively until values converge.
- This method has no limitation for device (GPU) capacity.

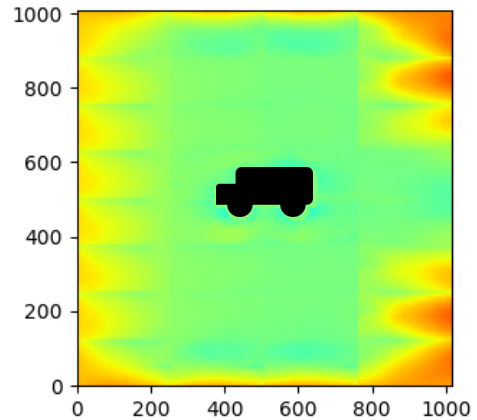


# Prediction results over a large computational domain

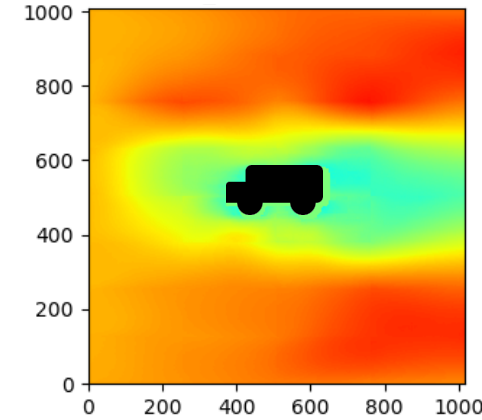
## CNN Prediction

**Initial Prediction**

**Velocity x**

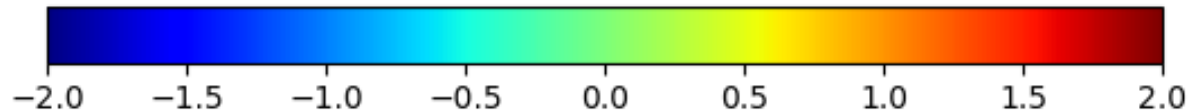
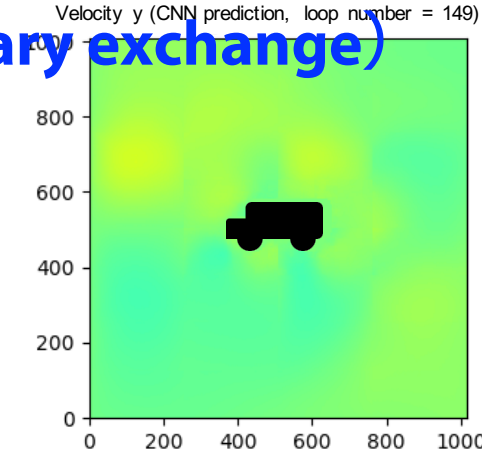
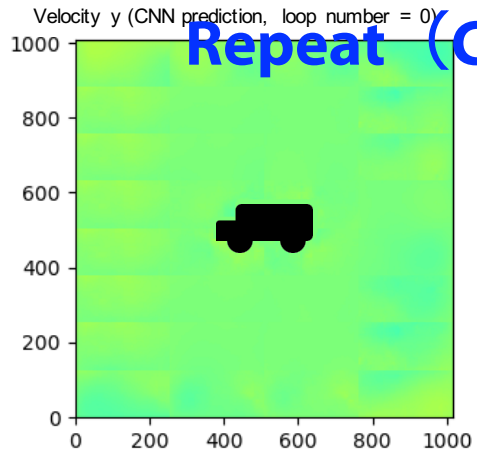


**Final (converged)**

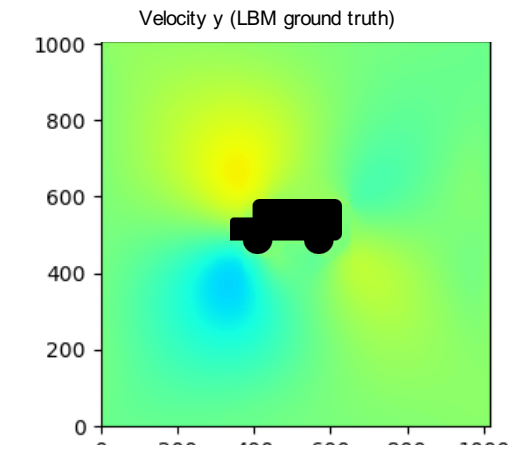
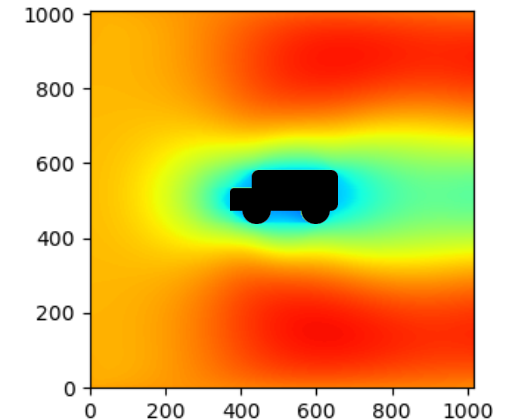


**Repeat (CNN + boundary exchange)**

**Velocity y**



## LBM Ground truth



4 x 8 subdomains

- We have developed deep learning fast surrogate for steady flow.
  - Predicting the LBM results by using convolutional neural networks (CNNs).
  - Predicting simulation results on large domain using CNNs with boundary exchange.
    - CNN and boundary exchange are performed iteratively until values converge.
    - The proposed method has no limitation for device (GPU) capacity.
    - The predicted results using 32 subdomains are shown.
- Future works
  - Extending the proposed methods to 3D CFD simulations.